

CS370 Operating Systems

Colorado State University

Yashwant K Malaiya

Fall 2024 Lecture 19



Virtual Memory

Slides based on

- Text by Silberschatz, Galvin, Gagne
- Various sources

Demand Paging

- Could bring entire process into memory at load time
- Or bring a page into memory only when it is needed: **Demand paging**
 - Less I/O needed, no unnecessary I/O
 - Less memory needed
 - Faster response
 - More users
- Similar to paging system with swapping
- Page is needed \Rightarrow reference to it
 - invalid reference \Rightarrow abort
 - not-in-memory \Rightarrow bring to memory
- “**Lazy swapper**” – never swaps a page into memory unless page will be needed
 - Swapper that deals with pages is a **pager**

Demand paging: Basic Concepts

- Demand paging: pager brings in only those pages into memory what are needed
- How to determine that set of pages?
 - Need new MMU functionality to implement demand paging
- If pages needed are already **memory resident**
 - No difference from non-demand-paging
- If page needed and not memory resident
 - Need to detect and load the page into memory from storage
 - Without changing program behavior
 - Without programmer needing to change code

Valid-Invalid Bit

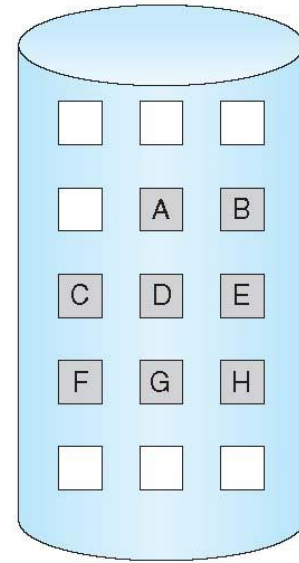
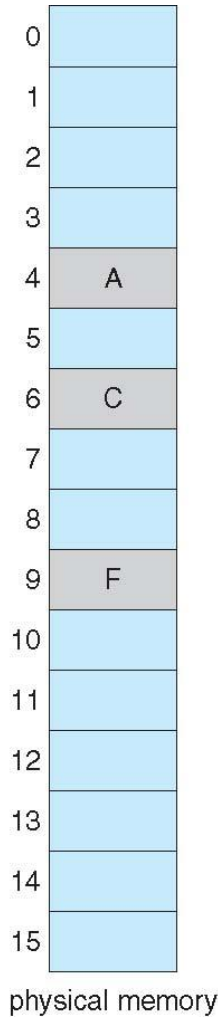
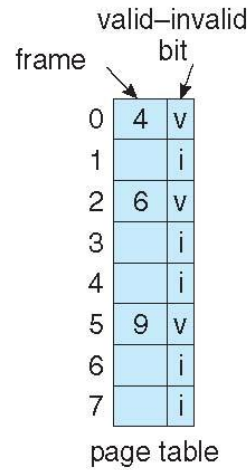
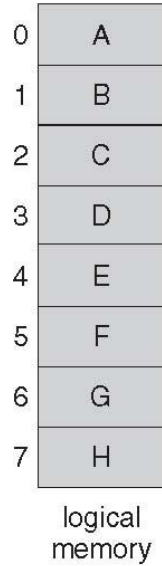
- With each page table entry a valid–invalid bit is associated (**v** \Rightarrow in-memory – **memory resident**, **i** \Rightarrow not-in-memory)
- Initially valid–invalid bit is set to **i** on all entries
- Example of a page table snapshot:

Frame #	valid-invalid bit
	v
	v
	v
	i
...	
	i
	i

page table

- During MMU address translation, if valid–invalid bit in page table entry is **i** \Rightarrow **page fault**

Page Table When Some Pages Are Not in Main Memory



Page 0 in Frame 4 (and disk)
Page 1 in Disk

Page Fault

- If there is a reference to a page, first reference to that page will trap to operating system: Page fault

Page fault

1. Operating system looks at a table to decide:
 - Invalid reference \Rightarrow abort
 - Just not in memory, but in *backing storage*, \rightarrow 2
2. Find free frame
3. Get page into frame via scheduled disk operation
4. Reset tables to indicate page now in memory
Set validation bit = **v**
5. Restart the instruction that caused the page fault

Page fault: context switch because disk access is needed

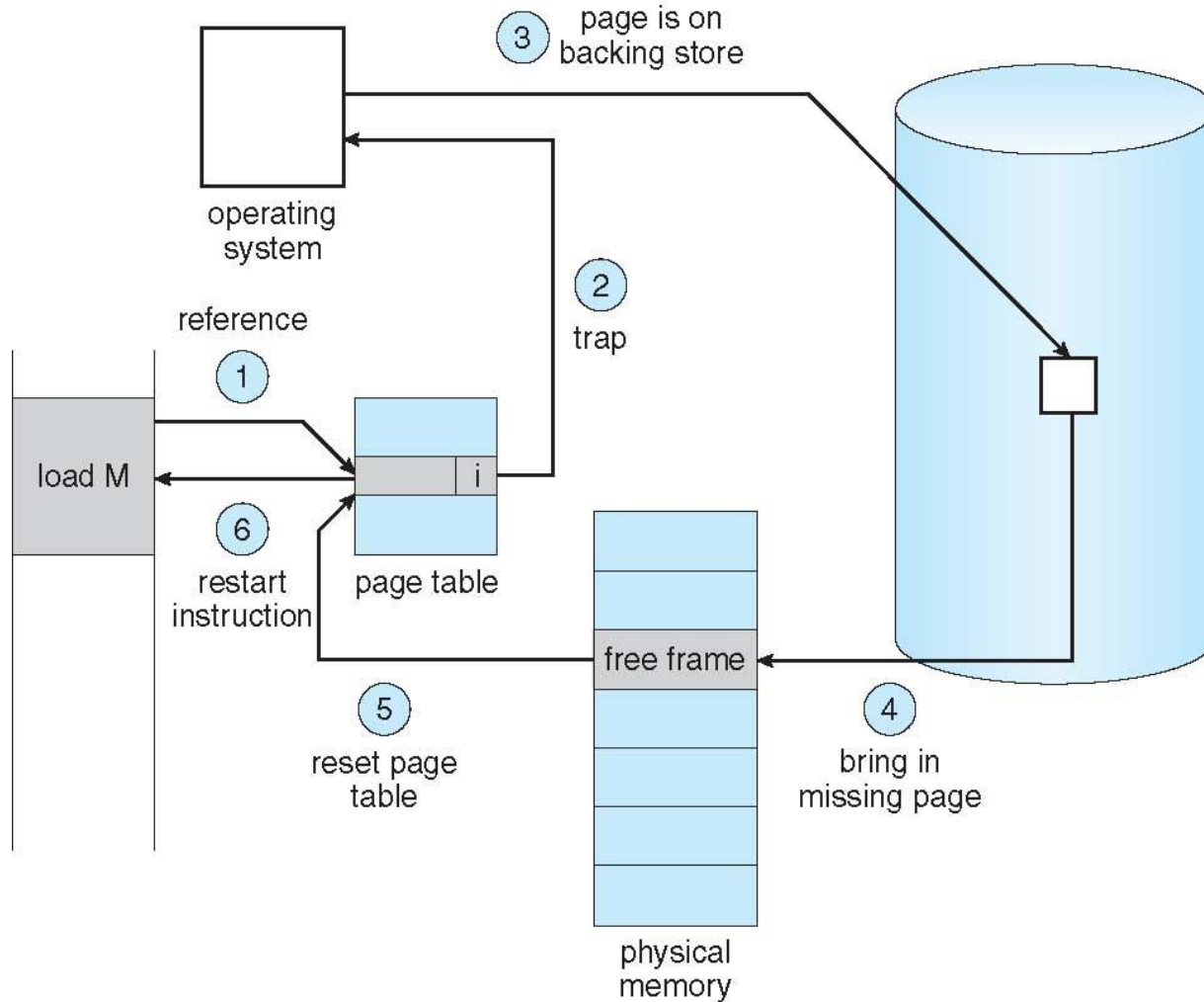
Technical Perspective: Multiprogramming



Solving a problem gives rise to a new class of problem:

- Contiguous allocation. **Problem:** external fragmentation
- Non-contiguous, but entire process in memory: **Problem:** Memory occupied by stuff needed only occasionally. Low degree of Multiprogramming.
- Demand Paging: **Problem:** page faults
- **How to minimize page faults?**

Steps in Handling a Page Fault



Stages in Demand Paging (worse case)

1. **Trap to the operating system**
2. Save the user registers and process state
3. Determine that the interrupt was a page fault
4. Check that the page reference was legal and determine the location of the page on the disk
5. **Issue a read from the disk to a free frame:**
 1. Wait in a queue for this device until the read request is serviced
 2. Wait for the device seek and/or latency time
 3. Begin the transfer of the page to a free frame
6. **While waiting, allocate the CPU to some other user**
7. Receive an interrupt from the disk I/O subsystem (I/O completed)
8. Save the registers and process state for the other user
9. Determine that the interrupt was from the disk
10. **Correct the page table and other tables to show page is now in memory**
11. Wait for the CPU to be allocated to this process again
12. Restore the user registers, process state, and new page table, and then **resume the interrupted instruction**

Performance of Demand Paging (Cont.)

- Three major activities
 - Service the interrupt – careful coding means just several hundred instructions needed
 - Read the page – relatively long time
 - Restart the process – again just a small amount of time
- Page Fault Rate $0 \leq p \leq 1$
 - if $p = 0$ no page faults
 - if $p = 1$, every reference is a fault
- Effective Access Time (EAT)

Hopefully $p \ll 1$

$$\text{EAT} = (1 - p) \times \text{memory access time} \\ + p (\text{page fault overhead} \\ + \text{swap page out} + \text{swap page in})$$

Page swap time = seek time + latency time

Demand Paging **Simple Numerical Example**

- Memory access time = 200 **nanoseconds**
- Average page-fault service time = 8 **milliseconds**
- $EAT = (1 - p) \times 200 \text{ ns} + p (8 \text{ milliseconds})$
 $= (1 - p) \times 200 + p \times 8,000,000 \text{ nanosec.}$
 $= 200 + p \times 7,999,800 \text{ ns}$

Linear with page
fault rate

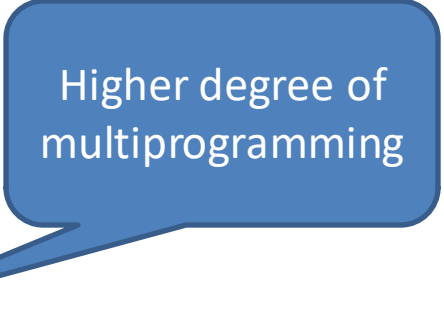
- If one access out of 1,000 causes a page fault, then
EAT = 8.2 microseconds.
This is a slowdown by a factor of 40!!
- **If want performance degradation < 10 percent, $p = ?$**
 - $220 > 200 + 7,999,800 \times p$
 $20 > 7,999,800 \times p$
 - $p < .0000025$
 - < one page fault in every 400,000 memory accesses

We make some simplifying assumptions here.

- Memory used for holding **program** pages
- **I/O buffers** also consume a big chunk of memory
- Choices:
 - Fixed percentage set aside for I/O buffers or
 - Processes and the I/O subsystem compete

Demand paging and the limits of logical memory

- Without demand paging
 - All pages of process **must be** in physical memory
 - Logical memory **limited** to size of physical memory
- With demand paging
 - All pages of process **need not be** in physical memory
 - Size of logical address space is **no longer constrained** by physical memory
- Example
 - 40 pages of physical memory
 - 6 processes each of which is 10 pages in size
 - But each process only needs 5 pages *as of now*
 - Run 6 processes with 10 pages to spare



Higher degree of multiprogramming

Coping with over-allocation of memory

Example

- Physical memory = 40 pages
- 6 processes each of which is of size 10 pages
 - But are using 5 pages each as of now
- What happens if each process needs all 10 pages?
 - 60 physical frames needed
- **Option: Terminate** a user process
 - But paging should be transparent to the user
- **Option: Swap out** a process
 - Reduces the degree of multiprogramming
- **Option: Page replacement:** selected pages.
Policy?



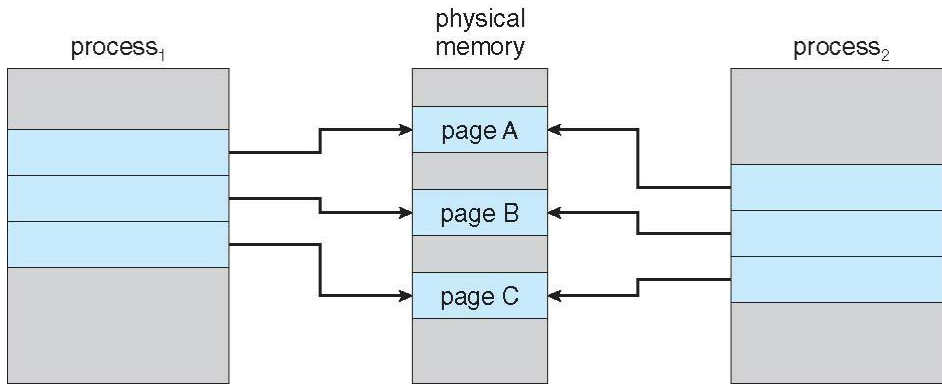
Solving the Fork mystery (Copy-on-Write)

- **Copy-on-Write** (COW) allows both parent and child processes to initially *share* the same pages in memory
 - If either process modifies a shared page, only then is page copied
- COW allows more efficient process creation as only modified pages are copied
- In general, free pages are allocated from a **pool** of **zero-fill on-demand** pages
 - Pool should always have free frames for fast demand page execution
 - Don't want to have to free a frame as well as other processing on page fault
 - Why zero-out a page before allocating it? (**security**)

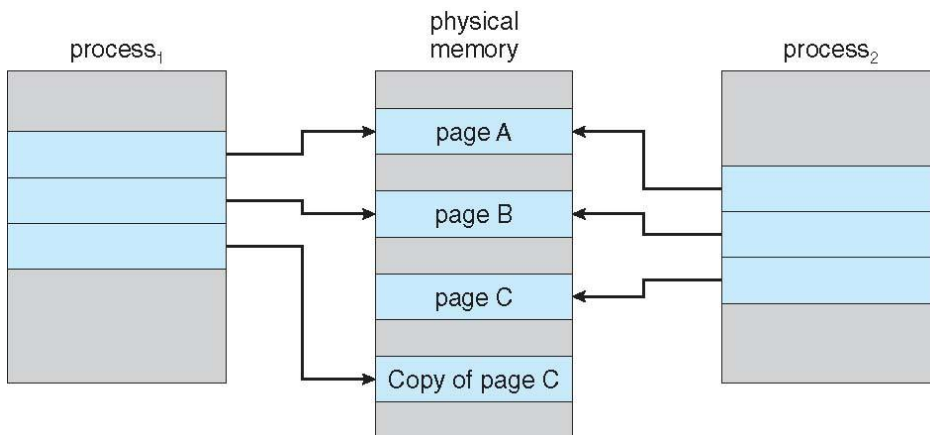
For
security

Copy-on-write

Before Process 1 Modifies Page C



After Process 1 Modifies Page C



What Happens if there is no Free Frame?

- Could be all used up by process pages or kernel, I/O buffers, etc
 - How much to allocate to each?
- Page replacement – find some page in memory, but not really in use, page it out
 - Algorithm – terminate? swap out? replace the page?
 - Performance – want an algorithm which will result in minimum number of page faults
- Same page may be brought into memory several times

Continued to Page replacement etc...

Page Replacement

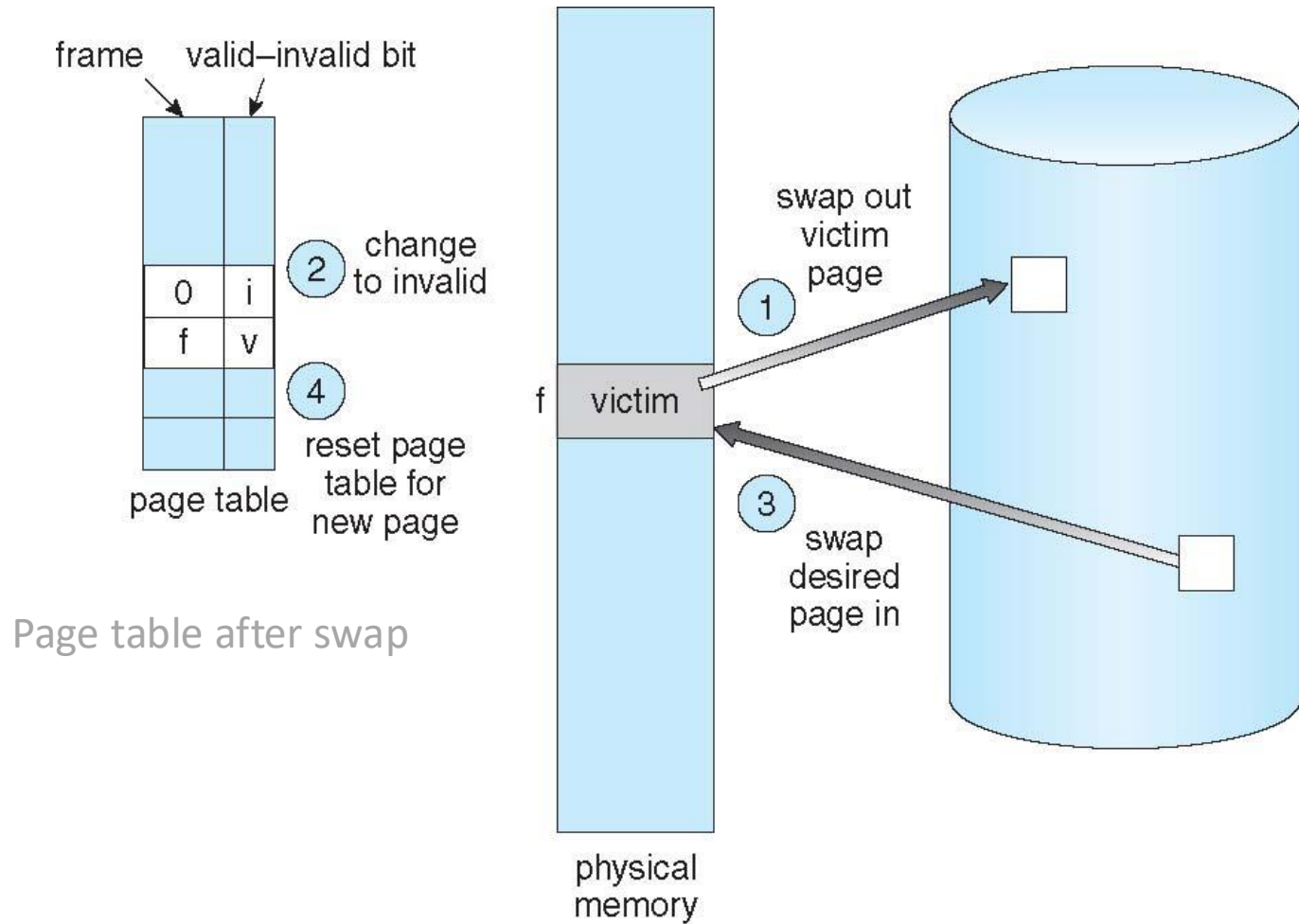
- Prevent **over-allocation** of memory by modifying page-fault service routine to include page replacement
- Page replacement completes separation between logical memory and physical memory – large virtual memory can be provided on a smaller physical memory
- Use **modify (dirty) bit** to reduce overhead of page transfers – only modified pages are written to disk

Basic Page Replacement

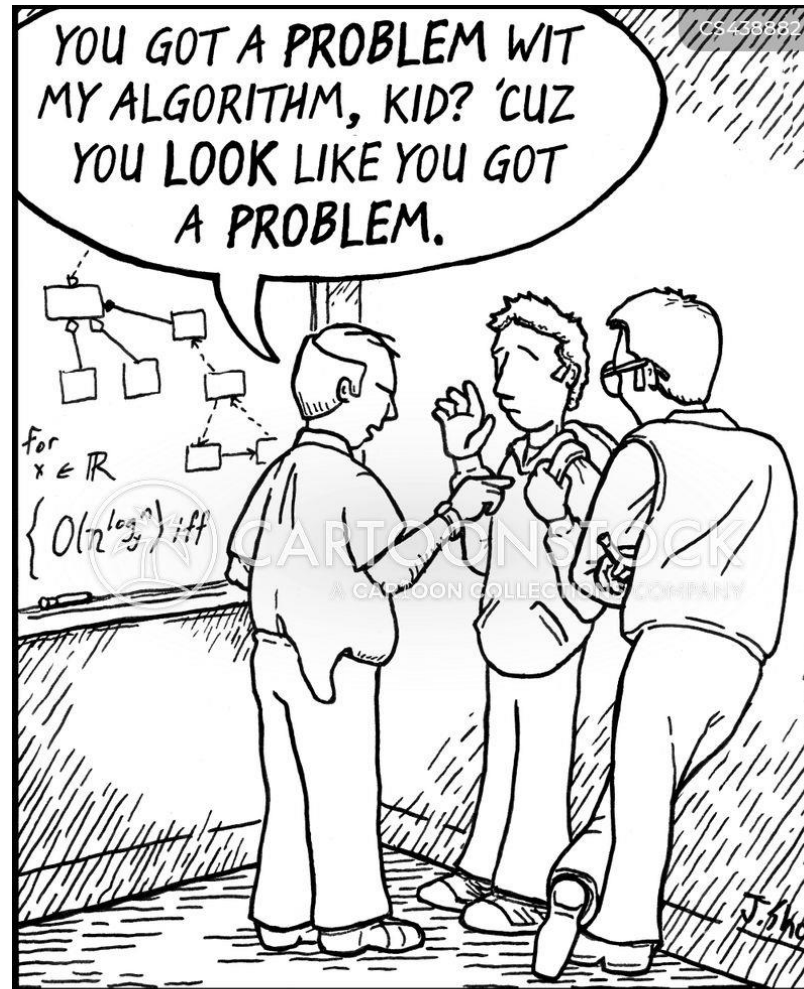
1. Find the location of the desired page on disk
2. Find a free frame:
 - I. If there is a free frame, use it
 - II. If there is no free frame, use a page replacement algorithm to select a **victim frame**
 - III. Write victim frame to disk if dirty
3. Bring the desired page into the (newly) free frame; update the page and frame tables
4. Continue the process by restarting the instruction that caused the trap

Note now potentially 2 page transfers for page fault – increasing EAT

Page Replacement



More algorithms ...



Jim unwittingly wanders into a rough section of the Computer Science department.

CS370 Operating Systems

Colorado State University

Yashwant K Malaiya

Spring 2022 Lecture 20



Virtual Memory

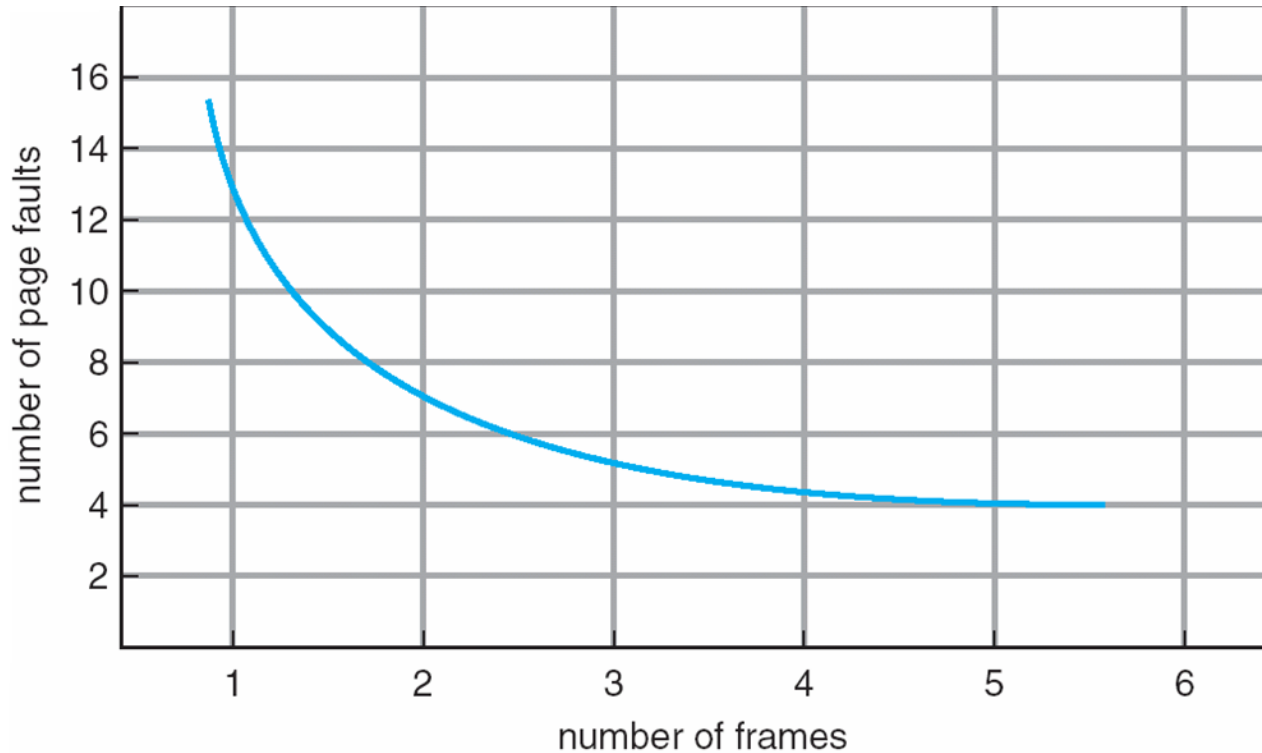
Slides based on

- Text by Silberschatz, Galvin, Gagne
- Various sources

Page Replacement Algorithms

- **Page-replacement algorithm**
 - Which frames to replace
 - Want lowest page-fault rate
- **Evaluate algorithm** by running it on a particular string of memory references (reference string) and computing the number of page faults on that string
 - String is just page numbers, not full addresses
 - Repeated access to the same page does not cause a page fault
 - Results depend on number of frames available
- In all our examples, we use **3** frames, and the **reference string** of referenced page numbers is
7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1

Graph of Page Faults Versus The Number of Frames



What we would generally expect

Page Replacement Algorithms

Algorithms

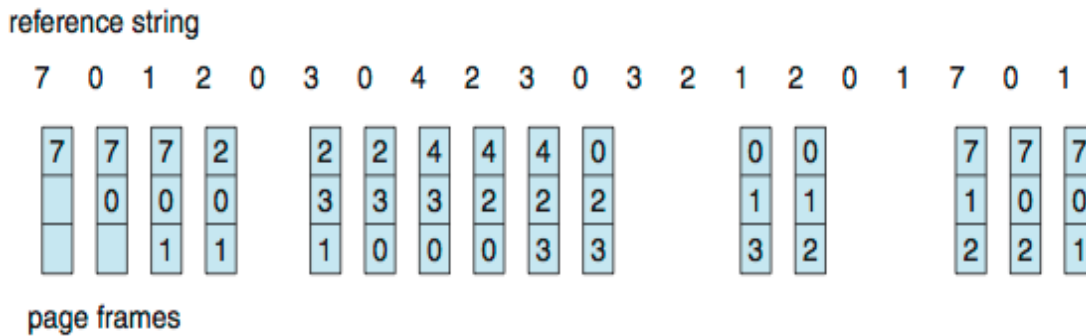
- FIFO
- “Optimal”
- The Least Recently Used (LRU)
 - Exact Implementations
 - Time of use field, Stack
 - Approximate implementations
 - Reference bit
 - Reference bit with shift register
 - Second chance: clock
 - Enhanced second chance: dirty or not?
- Other

FIFO page replacement algorithm: Out with the old; in with the new

- When a page must be replaced
 - Replace the oldest one
- OS maintains list of all pages currently in memory
 - Page at head of the list: Oldest one
 - Page at the tail: Recent arrival
- During a page fault
 - Page at the head is removed
 - New page added to the tail

First-In-First-Out (FIFO) Algorithm

- Reference string:
7,0,1,2,0,3,0,4,2,3,0,3,2,1,2,0,1,7,0,1
- 3 frames (3 pages can be in memory at a time per process)

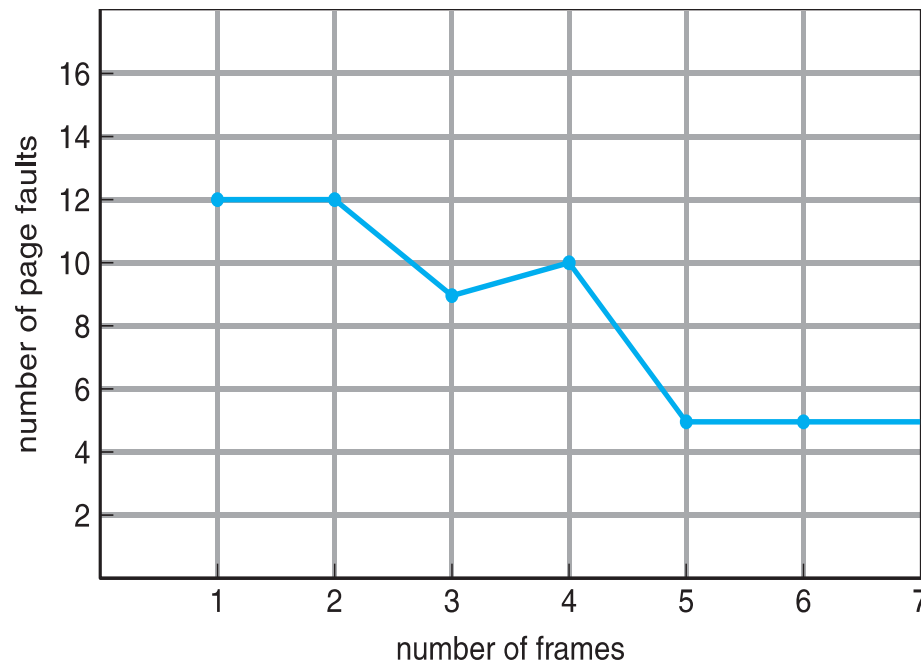


- 15 page faults (out of 20 accesses)
- Sometimes a page is needed soon after replacement 7,0,1,2,0,3 (0 out),0, ..

Belady's Anomaly

- Consider Page reference string **1,2,3,4,1,2,5,1,2,3,4,5**
 - 3 frames, 9 faults, 4 frames 10 faults! Try yourself.
 - Sometimes adding more frames can cause more page faults!

- **Belady's Anomaly**



Lazlo Belady was here at CSU. Guest in my CS530!



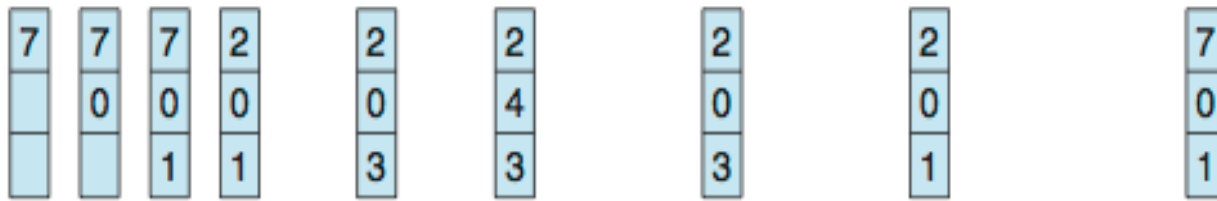
Budapest, 1928

“Optimal” Algorithm Belady 66

- Replace page that will not be used for longest period of time

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1



page frames

- 4th access: replace 7 because we will not use it for the longest time...
- 9 page replacements is optimal for the example
- But how do we know the future pages needed?
 - Can't read the future in reality.
- Used for *measuring* how well an algorithm performs.

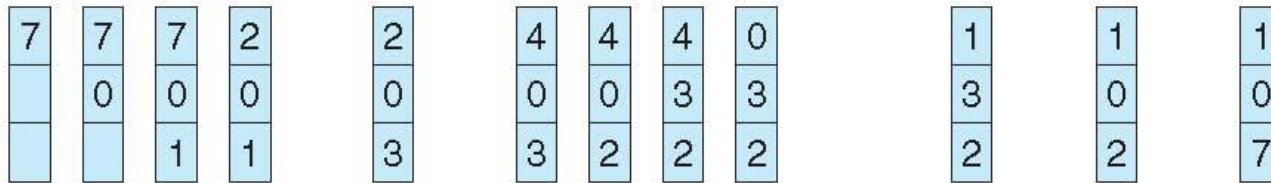
Least Recently Used (LRU) Algorithm

- Use past knowledge rather than future
- Replace page that has not been used in the most amount of time (4th access – page 7 is least recently used ...)
- Associate time of last use with each page

Track usage carefully!

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1



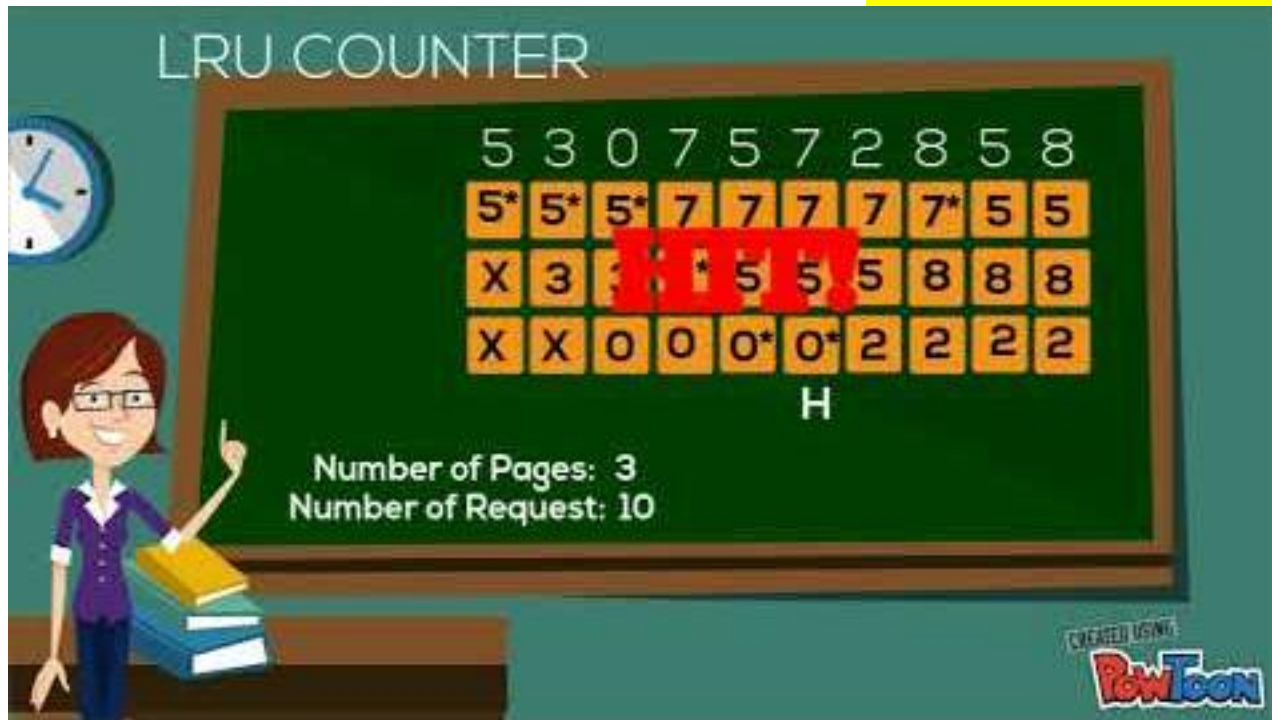
page frames

- 12 faults – better than FIFO (15) but worse than OPT (9)
- Generally good algorithm and frequently used
- But how to implement it by tracking the page usage?

LRU and OPT are cases of *stack algorithms* that don't have Belady's Anomaly

Least Recently Used (LRU) Algorithm

LRU page number is marked (*).
Unmarked if that page is accessed.



LRU applied to cache memory.

Least Recently Used (LRU) Algorithm

- * Use past knowledge rather than future
- 12 faults – better than FIFO (15) but worse than OPT (9)
- Tracking the page usage. One approach: mark least recently used page each time.

7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
7	7*	7*	2	2	2*	2*	4	4	4*	0	0	0*	1						
	0	0	0*	0	0	0	0	0*	3	3	3	3	3						
		1	1	1*	3	3	3*	2	2	2	2*	2	2						

- Other approach: use stack for tracking (soon)

LRU Algorithm: Implementations

Possible tracking implementations

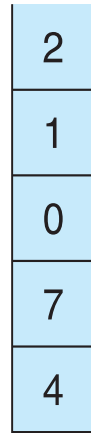
- Counter implementation
 - Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
 - When a page needs to be changed, look at the counters to find smallest value
 - Search through table needed
- Stack implementation
 - Keep a stack of page numbers in a double link form:
 - Page referenced:
 - move it to the top
 - requires 6 pointers to be changed
 - Each update expensive
 - No search for replacement needed (bottom is least recently used)

Use Of A Stack to Record Most Recent Page References

reference string

4 7 0 7 1 0 1 2 1 2 7 1 2

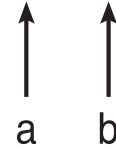
Most recently used ->



stack
before
a



stack
after
b



This shows tracking stack,
not actual frames.

Too slow if done in software

Use Of A Stack to Record Most Recent Page References

Examine this at home.

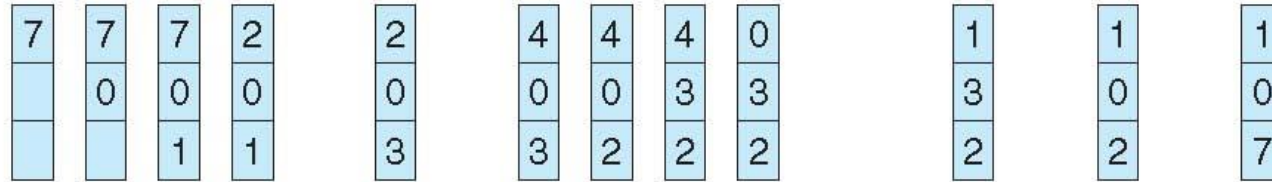
	4	7	0	7	1	0	1	2	1	2	7	1	2
Most recently used ->	4	7	0	7	1	0	1	2	1	2	7	1	2
		4	7	0	7	1	0	1	2	1	2	7	1
			4	4	0	7	7	0	0	0	1	2	7
					4	4	4	7	7	7	0	0	0
Least recently used ->								4	4	4	4	4	4

Detailed version of previous slide.
 This shows tracking stack, not actual frames.

Use Of A Stack to Record Most Recent Page References

reference string

7 0 1 2 0 3 0 4 2 3 0 3 2 1 2 0 1 7 0 1



page frames

Earlier problem (upper) revisited.
This shows tracking stack, not actual frames.

	7	0	1	2	0	3	0	4	2	3	0	3	2	1	2	0	1	7	0	1
MRU->	7	0	1	2	0	3	0	4	2	3	0	3								
		7	0	1	2	0	3	0	4	2	3	0								
LRU->			7	0	1	2	2	3	0	4	2	2								

LRU Approximation Algorithms

- LRU needs special hardware and still slow
- **Reference** 1 bit per frame to track history
 - With each page associate a bit, initially = 0
 - When the page is referenced, bit set to 1
 - Replace any page with reference bit = 0 (if one exists)
 - 0 implies not used since initialization
 - We do not know the order, however.
- Advanced schemes using more bits: preserve more information about the order

Ref bit + history shift register

LRU approximation 9 bits per frame to track history

Ref bit: 1 indicates used, Shift register records history. Examples:

Ref Bit	Shift Register	Shift Register after OS timer interrupt
1	0000 0000	1000 0000
1	1001 0001	1100 1000
0	0110 0011	0011 0001

- Interpret 8-bit bytes as **unsigned integers**
- Page with the lowest number is the LRU page: replace.

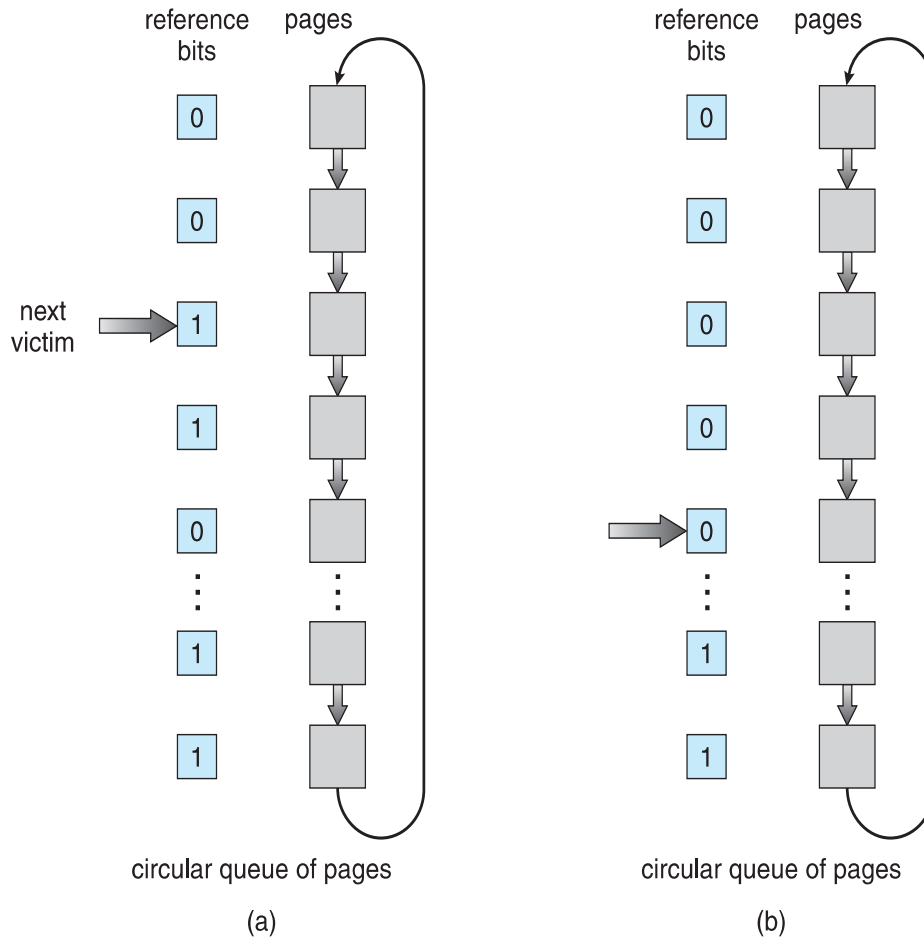
Examples:

- 00000000 : Not used in last 8 periods
- 01100101 : Used 4 times in the last 8 periods
- 11000100 used more recently than 01110111

Second-chance algorithm

- **Second-chance algorithm**
 - Generally FIFO, plus hardware-provided reference bit
 - Avoid throwing out a heavily used page
 - **“Clock”** replacement (using circular queue): hand as a pointer
 - Consider next page
 - Reference bit = 0 -> replace it
 - reference bit = 1 then: give it another chance
 - set reference bit 0, leave page in memory
 - consider next page, subject to same rules

Second-Chance (clock) Page-Replacement Algorithm



- **Clock** replacement: hand as a pointer
- Consider next page
 - Reference bit = 0 -> replace it
 - reference bit = 1 then:
 - set reference bit 0, leave page in memory
 - consider next page, subject to same rules

Example:

(a) Change to 0, give it another chance

(b) Already 0. Replace page

Enhanced Second-Chance Algorithm

Improve algorithm by using reference bit and modify bit (if available) in concert [clean page: better replacement candidate](#)

- Take ordered pair (reference, **modify**)
 1. (0, **0**) neither recently used not modified – best page to replace
 2. (0, **1**) not recently used but modified – not quite as good, must write out before replacement
 3. (**1**, **0**) recently used but clean – probably will be used again soon
 4. (**1**, **1**) recently used and modified – probably will be used again soon and need to write out before replacement
- When page replacement called for, use the clock scheme but use the four classes replace page in lowest non-empty class
 - Might need to search circular queue several times

Counting Algorithms

- Keep a counter of the number of references that have been made to each page
 - Not common
- **Least Frequently Used (LFU) Algorithm:** replaces page with smallest count
- **Most Frequently Used (MFU) Algorithm:** based on the argument that the page with the smallest count was probably just brought in and has yet to be used

Clever Techniques for enhancing Perf

- Keep a buffer (pool) of free frames, always
 - Then frame available when needed, not found at fault time
 - Read page into free frame and select victim to evict and add to free pool
 - **When convenient**, evict victim
- Keep list of modified pages
 - When backing store is **otherwise idle**, write pages there and set to non-dirty (**being proactive!**)
- Keep free frames' previous contents intact and note what is in them
 - If referenced again before reused, no need to load contents again from disk
 - Generally useful to reduce penalty if wrong victim frame selected

Buffering and applications

- Some applications (like databases) often understand their memory/disk usage better than the OS
 - Provide their own buffering schemes
 - If both the OS and the application were to buffer
 - Twice the I/O is being utilized for a given I/O
 - OS may provide “raw access” disk to special programs without file system services.